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Magnetic Interaction in Binuclear Copper(II) Complexes: Preparation and Structure of the Schiff Base Complex Derived From Pyrrole-Z-Carboxaldehyde and 3-Aminopropanol

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*Received August 10, 1971* 

*To obtain additional information about the relationship between magnetic properties and structure in oxygen-bridged complexes, the copper(II) complex of the Schifl base of pyrrole-2-carboxaldehyde and 3*  aminopropanol was prepared. The complex,  $\text{ICu}(C_{s-})$  $H_{10}N_2O$ )<sub>1</sub>, *crystallizes as monoclinic crystals (a =*  $\frac{1}{2}$ 25.61Å,  $b = 5.46\text{\AA}$ ,  $c = 16.90\text{\AA}$ ,  $\beta = 136.33^{\circ}$ ) of space *group C2fc with 8 formula units (4 dimers) per unit*  cell  $(\rho_{obsd} = 1.73, \rho_{calcd} = 1.74 \text{ g/cm}^3)$ . A total of *858 unique, non-zero reflections were obtained from precession camera photographs; the structure was solved from Patterson and electron density maps and re*fined by least-squares methods to a ocnventional R *value of 0.076. The coordination of copper is squareplanar and the coordination of the bridging oxygen is also planar. Within the planar four-membered copper-oxygen ring, the angle at copper is 76"; a molecular orbital treatment* **of** *the ~-system suggests a relationship between this angle and the magnetic properties of binuctear copper(l1) complexes.* 

#### **Introduction**

As part of a general study of oxygen-bridged complexes, structures were reported' for the complexes of copper(I1) and imines of acetylacetone and aminoalcohols; the structures and properties of these complexes were found to differ markedly with the size of the imino-alkoxide chelate ring. The complex, Ia, of the imine of 2-aminoethanol, was found to be tetrameric with a normal magnetic moment at room temperature; the imine of 3-amino-l-propanol (abbreviated PIA in formulas) gave a complex, Ib, which was dimeric with a subnormal magnetic moment at room temperature. From these observations and from a

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(2) J.A. Bertrand, J.A. Kelley, and J.L. Breece, *Inorg. Chim. Acta, 4*,<br>
(3) H.L. Schafer, J.C. Morrow, and H.M. Smith, *J. Chem. Phys.*,<br>
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(7) B.T. Kilbourn and
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- 373 (1963).<br>- (12) A.T. Casey, B.F. Hoskins, and F.D. Williams, *Chem. Comm*.<br>904 (1970).

survey of other oxygen-bridged copper(H) complex $es<sub>12</sub><sup>2-12</sup>$  a general relationship between magnetic moments and the stereochemistry of the bridging oxygen was suggested - complexes with tetrahedral coordination about oxygen exhibit normal magnetic moments at room temperature and complexes with planar threecoordination about oxygen exhibit low magnetic moments. On the basis of these observations, an explanation of the spin coupling in  $[Cu(PIA)]_2$ , Ib, in terms of a delocalized  $\pi$ -system involving the 3d<sub>xz</sub>,  $3d_{yz}$  orbital of the coppers and the  $2p_z$  orbitals of the oxygens was suggested.'

In order to investigate further the effect of factors such as ring size and the extent of delocalization on structure and magnetic properties, we have prepared a complex, II, with a five-membered unsaturated ring and a six-membered saturated ring; in this paper we report the preparation, structure and properties of that complex.



# **Experimental Section**

*Preparation.* Equimolar amounts (0.005 moles) of 3-amino-1-propanol and pyrrole-2-carboxaldehyde were mixed and dissolved in methanol. The above solution and a methanol solution containing 0.005 moles of potassium hydroxide were added simultaneously from dropping funnels to a warm stirred methanol solution of 0.005 moles of copper(II) acetate monohydrate. The resulting red-brown powder was allowed to air dry and then recrystallized from nitro-benzene; red needle-like crystals were obtained.

*Anal.* Calcd for  $Cu(C_8H_{10}N_2O)$ : C, 44.96; H, 4.72; N, 13.11. Found: C, 44.57: H, 5.05; N, 12.93.

*Magnetic Susceptibility Measurement.* The magnetic susceptibility of the compound was determined by

the Faraday method at  $26.5^{\circ}$ C, using HgCo(CNS)<sub>4</sub> as a calibrant. Diamagnetic corrections were made using published atomc values.<sup>13</sup> For Cu(C<sub>8</sub>H<sub>10</sub>N<sub>2</sub>O):  $\chi_{g}$  =  $0.17 \times 10^{-6}$ ,  $\chi_{\rm m}^{\rm corr}$  = 1200 × 10<sup>-6</sup>, and  $\mu_{\rm eff}$  = 0.54 B.M. per gram atom of copper(I1).

*Collection and Reduction of X-ray Data.* A crystal of approximate dimensions  $0.1 \times 0.1 \times 0.4$  mm was mounted along the long dimension (b-axis) on a glass fiber. Precession photographs were taken, using Zirconium-filtered Mo K $\alpha$  radiation,  $\lambda = 0.7106$ Å. The crystal was found to be monoclinic with a  $=$ 25.61(2)  $\AA$ ,<sup>14</sup> b = 5.46(1)  $\AA$ , c = 16.90(2), and  $\beta$  = 136.33(10)" at 25°C. The density calculated on the basis of 8 formula units per unit cell,  $1.74$  g/cm<sup>3</sup>, agrees well with the experimental value,  $1.73(1)$  g/ cm3, obtained by the flotation method using a mixture of carbon tetrachloride and diiodomethane.

The absence of *hkl* reflections with  $h+k = 2n+1$ and the absence of *k0l* reflections with  $l = 2n+1$  indicated space group Cc (No. 9) or C2/c (No. 15). The space group ambiguity was resolved in favor of C2/c through the Patterson map and the successful refinement of the structure.

Intensity data were collected on the precession camera, using the same crystal as used for the space group determination. A total of 858 unique non-zero reflections were estimated visually from the *hkl (1 =*   $O-4$ ) and the *hkl* ( $h = O-6$ ) layers. Lorentz-polarization corrections were computed but no corrections for absorption were made ( $\mu = 27$  cm<sup>-1</sup>).

*Solution and Refinement of Structure.* Computation were carried out on the Univac 1108 computer; programs employed included modified versions of Zalkin's FORDAP Fourier summation program, the Busing-Martin-Levy XFLS and ORFFE least squares, Johnson's ORTEP program for crystal structure illustrations, and various locally written programs.

The coordinates of the copper atoms were determined from a three-dimensional Patterson synthesis; after least-squares refinement of individual scale factors for each layer of data and the copper coordinates. a Fourier synthesis, phased on the copper atom, revealed the positions of all non-hydrogen atoms.

A Fourier synthesis phased on these atoms showed a definite anisotropic thermal motion of the copper atom; anisotropic thermal parameters were therefore assigned to the copper atom. At this point further structure-factor calculations and a difference Fourier phased on all the non-hydrogen atoms revealed the positions of all hydrogen atoms. All hydrogen atoms were introduced into the structure factor calculations with the isotropic temperature factor of the adjacent carbon; further full-matrix least-squares refinement (minimizing  $\omega (|F_o| - |F_e|)^2$ ) of all parameters except hydrogen coordinates and hydrogen temperature factors converged to a conventional  $R_1$  value  $(\Sigma || F_{\circ}] \left| \int F_c \right| / \sum \left| F_o \right|$ ) of 0.076 and a value of R<sub>2</sub> ( $\sum \omega$ )  $\left| F_o \right|$  - $|F_c|/2/\Sigma \omega (|F_o|)^2$ <sup>1/2</sup>) equal to 0.076 with all reflections weighted at unity. In the final cycle of refinement,

(13) B.N. Figgis and J. Lewis in « Modern Coordination Chemistry » J. Lewis and R.G. Wilkins, Ed., Intersciences Publishers, Inc., John Wiley and Sons, Inc., New York, N.Y., 1960, p. 403.<br>Wiley and Sons, Inc., New York, N

there was no parameter shift greater than  $1/10$  of one esd. A final difference Fourier had no positive maxima greater than  $0.5 \text{ e}/\text{\AA}^3$ .

In the structure factor calculations, the scattering factors tabulated by Ibers<sup>15</sup> were employed for all atoms.

The positional and thermal parameters derived from the last cycle of least-squares refinement are presented in Table I; the observed and calculated structure factors are given in Table II.

**Table** I. Final Positional and Thermal Parameters for  $[ Cu(C<sub>8</sub>H<sub>10</sub>N<sub>2</sub>O) ].$ 

Atom	x	у	z	$B, \mathbf{A}^2$
Cu	0.2382(1)	0.0620(2)	0.0507(1)	$2.2(1)^{a}$
O	0.3139(4)	0.194(1)	0.0641(6)	2.4(1)
N <sub>1</sub>	0.1665(5)	0.063(2)	0.0489(8)	2.9(2)
N2	0.3005(5)	$-0.209(1)$	0.1564(8)	2.7(2)
C1	0.3901(6)	0.108(2)	0.1389(9)	2.6(2)
C <sub>2</sub>	0.4185(5)	$-0.014(2)$	0.2468(9)	2.7(2)
C <sub>3</sub>	0.3792(6)	$-0.253(2)$	0.2182(9)	2.6(2)
C4	0.2668(6)	$-0.342(2)$	0.172(1)	2.7(2)
C <sub>5</sub>	0.1924(6)	$-0.266(2)$	0.111(1)	2.6(2)
C <sub>6</sub>	0.1401(6)	$-0.365(2)$	0.105(1)	3.2(2)
C7	0.0765(7)	$-0.207(2)$	0.035(1)	4.2(3)
C8	0.0967(6)	$-0.023(2)$	0.003(1)	3.6(3)
H1C1	0.397	$\rm -0.010$	0.104	
H2C1	0.431	0.240	0.175	
H <sub>1</sub> C <sub>2</sub>	0.464	-0.060	0.323	
H <sub>2</sub> C <sub>2</sub>	0.400	0.100	0.275	
H1C3	0.380	-0.365	0.175	
H2C3	0.402	$-0.332$	0.289	
HC <sub>4</sub>	0.290	$-0.500$	0.230	
HC <sub>6</sub>	0.140	$-0.520$	0.140	
HC7	0.024	-0.200	0.001	
HC8	0.055	0.100	0.058	

n Anisotropic refinement of the thermal parameter of copper gave the expression:  $exp[-(16h^2+189k^2+47l^2+14h^2])]$  $+36kl$ ) $\times$  10<sup>-4</sup>]

## **Discussion**

The structure, Figure 1, consists of dimeric units; the coppers of the dimer are bridged by oxygens of the iminoalkoxide ligands. Interatomic distances and angles are given in Table III; selected least-squares planes are presented in Table IV. The copper is four coordinate and the copper and the four atoms bonded to copper are close to planar with none of the five more than 0.11 A out of the best least-squares plane through 0,Nl ,N2, and 0'. The angles at copper are not the 90" angles expected for square-planar coordination but reflect the effect of ring size - the larger N-Cu-O angle  $(106.0(4)°)$  is not included in a ring, the other  $N-Cu-O$  angle  $(95.2(4)^\circ)$  is in the sixmembered chelate ring, the N-Cu-N angle (83.2(5)°) is in the five-membered chelate ring, and the 0-Cu-0 angle  $(76.1(4)°)$  is in the four-membered copperoxygen ring. The four-membered copper-oxygen ring is exactly planar since there is an inversion center at the center of the ring; the coordination around the bridging oxygen is issentially planar with the carbon bonded to oxygen only 0.05 A out of the plane of the

(15) J.A. Ibers in « International Tables for X-Ray Crystallography », Vol. 3, the Kynoch Press, Birminghan, England, 1962.

four-membered ring. The five-membered delccalized chelate ring is essential!y planar with no atom of the ring more than 0.02 A out of the best least-squares plane through the ring; the five-membered pyrrole ring is planar to within 0.01 A.



Figure 1. ORTEP plot of the molecular structure of  $Cu(C_{\rm s}H_{10}N_2O)$ . The thermal ellipsoids and spheres are at The thermal ellipsoids and spheres are at the 50% probability level.

As in other polynuclear structures in which the coordination of the bridging oxygen is planar, the room temperature magnetic moment (0.54 B.M.) is considerably below the value expected for one unpaired electron per copper. An explanation of the spin-coupling in such systems in terms of a delocalized  $\pi$ -system involving the 3d<sub>xz</sub>, 3d<sub>yz</sub> orbitals of the coppers and the 2p, orbitals of the oxygens has been suggested. A molecular orbital treatment of these

six orbitals indicates two anti-bonding orbitals of different symmetries; since these orbitals can, thus, have different energies, it is possible for the dimer to have a singlet ground state and a thermally accessible rriplet state.

Although the energy difference between the antibonding  $\pi$ -orbitals of the present compound could result from interactions with the chelate  $\pi$ -system, the reason for an energy difference between the corresponding  $\pi$ -orbitals of complexes such as  $[Cu(PyO)$ - $Cl<sub>2</sub>$ ]<sub>2</sub> (where PyO represents pyridine-N-oxide), which also exhibit sub-normal magnetic moments at room temperature,<sup>16</sup> was not apparent from the previous treatment. Furthermore, planar four-membered rings are also present in chloride-bridged complexes of copper(I1) and the room temperature moments of those compounds are normal. A review of the available structure data on oxygen-bridged<sup>1-12</sup> and chloridebridged<sup>17-22</sup> complexes of copper(II) reveals an important difference: in all of the oxygen-bridged complexes with sub-normal room temperature magnetic moments the 0-Cu-0 angles within the four-membered ring are considerably less than 90" (usually near 70"); in the chloride-bridged complexes, the Cl-Cu-Cl

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1037 (1963).<br>
(197) R.D. Willet, C. Dwiggins, Jr., R.F. Kruh, and R.E. Rundle<br>
1. Chem. Phys., 38, 2429 (1953).<br>
(20) R.D. Willett and R.E. Rundle, J. Chem. Phys., 40, 838 (1964).<br>
(21) R.S. Sager and W.H. Watson, *Inerg.* 



Table II. Observed and Calculated Structure Factors (in Electrons) for  $\lceil Cu(C_sH_0N,0) \rceil$ ,

<sup>(16)</sup> J.V. Quagliano, J. Fujito, G. Frantz, D.J. Phillips, J.A. Walmsley, and S.Y. Tyree, *J. Am. Chem. Soc.*, 83, 3770 (1961).<br>
(17) P.H. Vossos, L.D. Jennings, and R.E. Rundle, *J. Chem. Phys.*, 1590 (1960).<br>
(18) P.H. Vo

	Distance,		Angle,
Atoms	A	Atoms	degrees
Cu-Cu'	3.001((4)	$Cu-N1-C5$	110.7(9)
$Cu-O$	1.920(11)	$C5-N1-C8$	106.9(12)
$Cu-O'$	1.891(7)	$Cu-N1-C8$	142.2(9)
$Cu-N1$	1.942(13)	N1-C8-C7	111.1(11)
$Cu-N2$	1.952(9)	C6-C7-C8	103.7(14)
$O-C1$	1.435(13)	C5-C6-C7	107.0(12)
N <sub>1</sub> -C <sub>5</sub>	1.328(14)	N1-C5-C6	111.3(11)
<b>N1-C8</b>	1.353(18)	N1-C5-C4	117.4(13)
$N2-C3$	1.472(16)	C4-C5-C6	131.3(11)
$N2-C4$	1.293(20)	N <sub>2</sub> -C <sub>4</sub> -C <sub>5</sub>	115.4(10)
$C1-C2$	1.543(20)	$Cu-N2-C4$	113.0(8)
$C2-C3$	1.499(15)	$Cu-N2-C3$	124.5(9)
C <sub>4</sub> -C <sub>5</sub>	1.420(17)	$C3-N2-C4$	122.4(9)
$C5-C6$	1.379(24)	N2-C3-C2	109.9(9)
$CG-C7$	1.414(16)	$C1-C2-C3$	111.3(9)
$C7-C8$	1.410(23)	$O-C1-C2$	111.2(13)
$C1-H1C1$	0.97	$Cu-O-C1$	126.4(7)
$C1-H2C1$	1.03	Cu-O-Cu'	103.9(4)
C <sub>2</sub> -H <sub>1</sub> C <sub>2</sub>	0.95	$C1-O-Cu'$	129.6(9)
C <sub>2</sub> -H <sub>2</sub> C <sub>2</sub>	1.08	$O-Cu-N2$	95.2(4)
C3-H1C3	0.96	$N1$ -Cu-N2	83.2(5)
C3-H2C3	0.97	N1-Cu-O'	106.0(4)
$C4-HC4$	1.10	$O-Cu-O'$	76.1(4)
C <sub>6</sub> -HC <sub>6</sub>	1.03	O-C1-H1C1	114
C7-HC7	1.01	H1C1-C1-H2C1	106
C8-HC8	1.03	C <sub>2</sub> -C <sub>1</sub> -H <sub>2</sub> C <sub>1</sub>	101
		C1-C2-H1C2	141
		H1C2-C2-H2C2	93
		C3-C2-H2C2	104
		C <sub>2</sub> -C <sub>3</sub> -H <sub>1</sub> C <sub>3</sub>	115
		H1C3-C3-H2C3	109
		N2-C3-H2C3	104
		N2-C4-HC4	128
		C5-C4-HC4	117
		C5-C6-HC6	133
		C7-C6-HC6	120
		C6-C7-HC7	139
		C8-C7-HC7	117
		C7-C8-HC8	117
		<b>N1-C8-HC8</b>	132

Table III. Interatomic Distances and Angles for  $[ Cu(C_{8}H_{10}N_{2}O)]_{2}.$ 





(b) Equation of the Least-Squares Plane  $b$  of the Coordination Sphere (O,Nl,N2,0'):

## $0.205X - 0.410Y - 0.888Z = 0.749$



a Direction cosines of the plane refer to the orthogonal axis system  $a,b,c^*$ .  $b$  All atoms weighted at unity.

angles approach 90". By incorporating these observations into the treatment of the  $p\pi - d\pi$  system, it is possible to give an explanation of the energy difference between the anti-bonding orbitals in all of the oxygen-bridged copper(II) complexes that show sub-<br>normal room temperature magnetic moments. The normal room temperature magnetic moments. treatment employed has been presented previously<sup>23-25</sup> in a general treatment of  $p\pi-\bar{d}\pi$  systems but has not been applied to transition metal complexes.

Although the actual symmetry of the complexes is usually lower, the four-membered ring in several of the low-moment compounds approaches  $D_{2h}$  symmetry. Using the coordinate system previously suggested<sup>3</sup>, the six  $\pi$ -orbitals, Figure 2, transform in  $D_{2h}$  symmetry as  $A_u + B_{2g} + 2B_{1u} + 2B_{3g}$ ; suitable combinations of atomic orbitals which transform with these symmetries are indicated in Figure 3. Of these, the  $A_u$  and  $B_{2g}$  combinations are non-bonding and there are bonding and anti-bonding combinations with both  $B_{1u}$  and  $B_{3g}$  symmetries.

Considerations of the  $B_{1u}$  and  $B_{3g}$  combinations indicates that the two would have identical overlap of copper and oxygen orbitals for an 0-Cu-0 angle of 90"; however, as the 0-Cu-0 angle is decreased, the



Figure 2. Projection of the six  $\pi$ -orbitals onto the xy plane.



Figure 3. Symmetry adapted linear combinations of atomic orbitals.

(23) K.A.R. Mitchell, *Chem. Revs.*, 69, 157 (1969).<br>
(24) D.P. Craig, Special Publication No. 12, The Chemical Society,<br>
London, 1958, p. 343.<br>
(25) D.P. Craig and K.A.R. Mitchell, *J. Chem. Soc.*, 4682 (1965).

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overlap of the  $B_{1u}$  combination is increased and that of the  $B_{3g}$  combination is decreased. For an O-Cu-O angle of 90°, the  $B_{1u}$  and  $B_{3g}$  anti-bonding orbitals would, therefore, have the same energy unless they were affected by other factors such as different interactions with a chelate  $\pi$ -system.

In addition to the dependence on the angle at copper, the energy separation would depend on the energies of the oxygen orbitals and the copper orbitals and, since these energies depend on the bonding to the rest of the molecule, the nature of the rest of the molecule would affect the magnitude of the energy difference. This factor is reflected in the variation of J, the coupling constant, with the electron density at oxygen as observed<sup>26</sup> for a series of complexes with substituted pyridine oxides as bridging groups; it also accounts for the difference in magnetic moments observed for compounds such as  $[\text{Cu}(\text{PIA})]_2^1$  and  $[\text{Cu}$ - $(PyO)Cl<sub>2</sub>1<sub>2</sub><sup>4</sup>$ , both of which have O-Cu-O angles of approximately 72".

The above treatment appears to qualitatively explain the observed magnetic moments of oxygen-bridged copper(I1) complexes; it is also possible to show that such a treatment gives singlet-triplet separations of the right magnitude. Experimental values are available - the temperature dependence of the magnetic susceptibilites *ol* a number of oxygen-bridged cop $per(II)$  dimers have been studied<sup>26-28</sup> and have been found to fit the equation<sup>29</sup>:

$$
\chi_M = (2g^2\beta^2N/3kT)\left[1 + 1/3exp(J/kT)\right]^{-1} + N\alpha
$$

where  $\chi_M$  is the molar susceptibility of the dimer, g is the Lande factor,  $\beta$  is the Bohr magneton, N, is Avogadro's number, k is the Boltzmann constant,  $N\alpha$ is the temperature independent paramagnetism, and J is the singlet-triplet energy separation. Values for J have usually been less than 500 cm<sup>-1</sup>; from the room temperature susceptibility of  $[Cu(C_8H_{10}N_2O)]_2$  $(0.54 \text{ B.M.})$  a J value of ca. 560 cm<sup>-1</sup> is obtained.

For purposes of energy calculations, it is convenient to write  $B_{1u}$  orbitals in terms of separate oxygen and copper orbitals:

$$
\varphi_1(B_{1u}) = (p_z + p_z') / \sqrt{2}
$$
  

$$
\varphi_2(B_{1u}) = (d_{xz} + d_{xz'}) / \sqrt{2}
$$

In terms of the general treatment<sup>23,24</sup>, these correspond to  $\varphi_0^A$  and  $\varphi_0^B$ . Using a Huckel approximation with the following definitions,

$$
H_{11} = \int \varphi_1 H \varphi_1 d\tau = \alpha
$$
  
\n
$$
H_{22} = \int \varphi_2 H \varphi_2 d\tau = \int d_{xx} H d_{xx} d\tau = \alpha_{xz}
$$
  
\n
$$
H_{21} = H_{12} = \int \varphi_1 H \varphi_2 d\tau = 1/2 \int (p_z + p_z') H (d_{xz} + d_{xz'}) d\tau = 2 \int p_z H d_{xz} d\tau = 2 \beta_{xz},
$$

the secular equation is:

$$
\begin{array}{ll}\n\alpha-\mathbf{E} & 2\beta_{xz} \\
2\beta_{xz} & \alpha_{xz}-\mathbf{E}\n\end{array} = 0
$$

(26) W.E. Hatfield and J.S. Pascal, *J. Am. Chem. Soc.*, 86, 3888 *(27)* W.E. Hatfield and F.L. Hunger, Inorg. C/tern., 5, 1161 (1966). (31) H.H. JalTe, I. Chcrn. *Phys.. 21.* 258 (1953).

and

$$
E = \frac{1}{2}(\alpha + \alpha_{xz} \pm [(\alpha - \alpha_{xz})^2 + 16\beta_{xz}^2]^{1/2}.
$$

For the  $B_{3g}$  orbitals, the appropriate linear combinations of oxygen and copper orbitals are:

$$
\begin{aligned} \phi_1(B_{3g}) &= (p_z - p_z') / \sqrt{2} \\ \phi_2(B_{3g}) &= i (d_{yz} - d_{yz'}) / \sqrt{2} \end{aligned}
$$

In terms of the general treatment<sup> $23,24$ </sup>, these correspond to  $\varphi_1^A$  and  $\varphi_1^B$ . Using the same definitions as before, the secular equation may be writen

> $\alpha$ -E  $2i\beta_{yz}$  $-2i\beta_{yz}$  $\alpha_{yz}$ -E  $=0$

and

$$
E = \frac{1}{2}(\alpha + \alpha_{yz} \pm [(\alpha - \alpha_{yz})^2 + 16\beta_{yz}^2]^{1/2}).
$$

Although  $\alpha_{xz}$  and  $\alpha_{yz}$  may differ due to interactions with the rest of the molecule, the difference in most compounds is probably not very large and we have used  $\alpha_{xz} = \alpha_{yz} = \alpha_d$ ; however, for an O–Cu–O angle other than 90°, different values are necessary for  $\beta_{xz}$ and  $\beta_{yz}$ . The energy difference, J, for the two antibonding orbitals is given by:

$$
J = \frac{1}{2} \left( \left[ (\alpha - \alpha_d)^2 + 16 \beta_{yz}^2 \right]^{1/2} + \left[ (\alpha - \alpha_d)^2 + 16 \beta_{xz}^2 \right]^{1/2} \right).
$$

Although there is considerable question about the numerical values to be used, we have used valence state ionization energies<sup>30</sup> for the  $\alpha$ 's; for the  $\beta$  values, we have. used

$$
\beta\!=\!S_{ij}(\alpha\!+\!\alpha_{\rm d})\!\cos\gamma
$$

where  $\gamma$  is the angle between Cu–O direction and the plane of the d orbital; the cos  $\gamma$  term was included<sup>23,24</sup> to account for the angular dependence of the overlap. The overlap integral was obtained from tabulated values<sup>31</sup> in the literature. With these values we calculate a J value of  $\left[\text{Cu}(C_8H_{10}H_2O)\right]_2$  (ca. 870 cm<sup>-1</sup>) which is of the same magnitude as the observed values.

It thus appears that the low room temperature magnetic moments of oxygen-bridged copper(II) complexes can be explained in terms of a delocalized  $\pi$ system; it is probable that the same explanation applies to complexes of other metal ions. The same explanation can also be used to explain the low moment observed for  $CuF_2$  since the F-Cu-F angle is 76°.

*Acknowledgments.* This work was supported by NSF Grant GP-20885. Funds from the Quality Improvement Program of the State of Georgia for the purchase of X-ray diffraction equipment are gratefully acknowledged; the help of the Rich Electronic Computer Center of Georgia Institute of Technology with computations is appreciated.

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